

MATH 267 (Sections A3, C-1) Homework No. 5

Reading

Section 4.5

Section 4.6

Section 4.7

Suggested Problems

Section 4.5, Exercises 3,7,15,25,27,31,33,41,43.

Section 4.6, Exercises 3,5,7

Section 4.7, Exercises 1, 9, 13, 15

Problems to be handed in (due Monday February 21-st)

Problem 1 (13 points)

Use the method of undetermined coefficients to find a particular solution of the following inhomogeneous linear O.D.E.

$$y'' - y' = t + e^t \cos(t).$$

Problem 2 (8 points)

Use the method of variation of parameters to find a particular solution of the following inhomogeneous linear O.D.E.

$$y'' - y' = e^t.$$

Problem 3 (9 points)

Consider the following forced harmonic motion for general forcing frequency ω :

$$x'' + 2x' + 4x = 3\cos(\omega t).$$

1. Write the **gain** $G(\omega)$ as a function of ω .
2. Write the **phase** $\phi(\omega)$ as a function of ω .
3. Write the **transfer function** $H(\omega)$ as a function of ω
4. Write the general solution as a function of ω and indicate the **steady state** and the **transient** term.