

3/03/2011

Began class reviewing Darcy's law,

$$J_w = -K(\theta_w) \frac{d\theta_w}{dz} + gK(\theta_w)$$

using figures from the text (Fig
and from Soil Science Simplified (SSS).
Note mistakes in vertical axes in the
SSS figure.

~~~~~ Guest lecture, Dr. Robert Horton

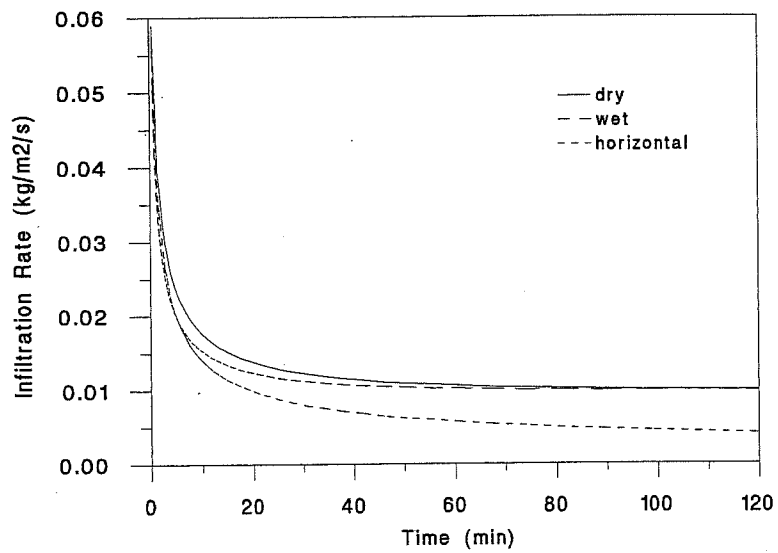
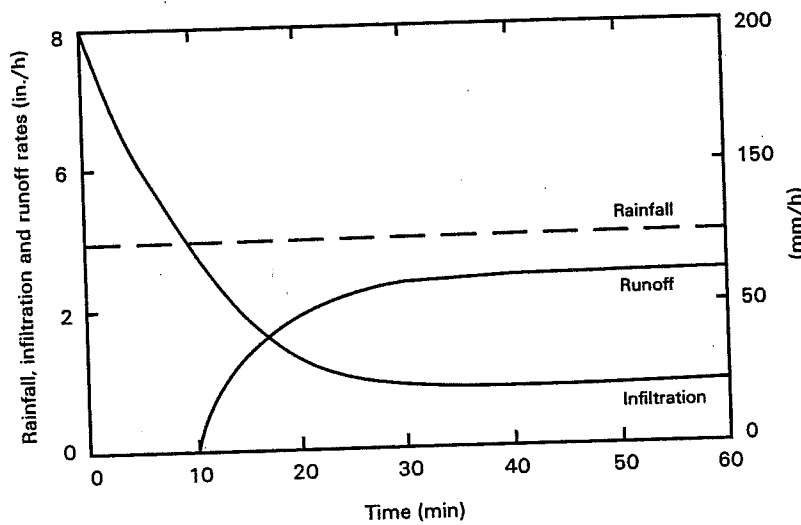
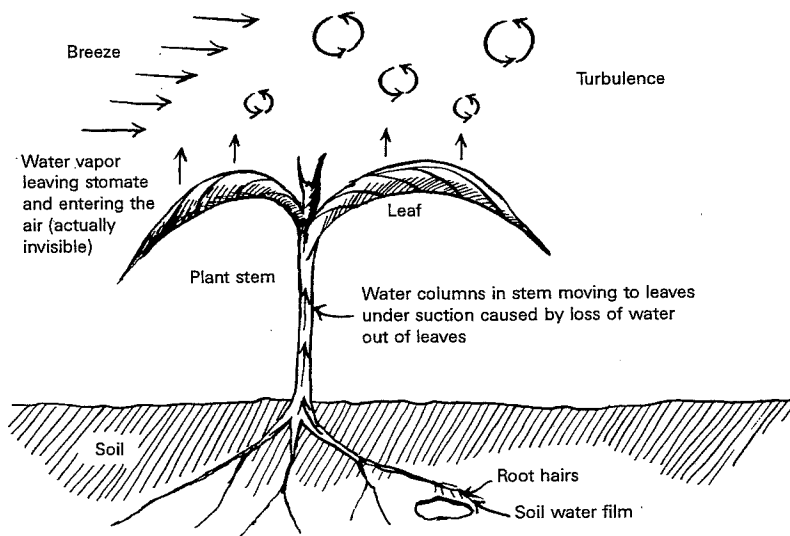


FIGURE 9.1. Vertical infiltration rate for water into initially dry and wet soil, and horizontal infiltration into dry soil.

**6.4.** Runoff and infiltration for a 1.5-inch (38-mm) rainfall in 1 hour. The infiltration rate decreases as the soil wets until runoff begins after 10 minutes. Late in the storm, the runoff and infiltration rates are steady. Runoff would have begun later and been less if the soil had a higher infiltration rate.



**6.12.** Water moves into the roots and through the plant primarily by capillary action.

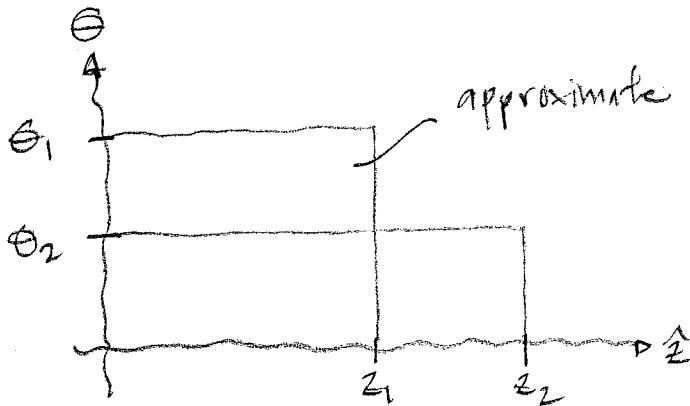


APK  
3/03/09

# Soil Water Redistribution

optional 3/03/2011

After a rain or irrigation event, the soil water profile continues to change as the water is redistributed.



area = depth of wetted profile  
× average water content

$$= D \times \Theta = d$$

= equivalent depth of water = constant

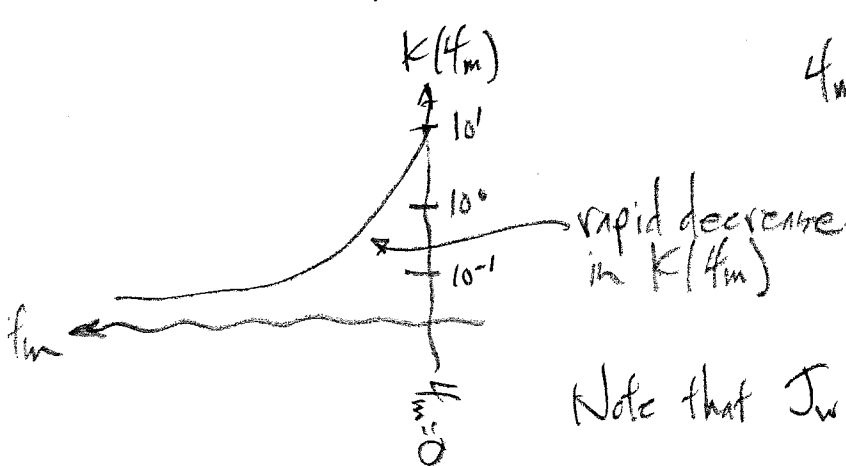
See Fig 9.3

The rectangle of wet soil changes shape but the area remains approximately constant as water is redistributed. *ask why this is an approximation*

When redistribution slows down significantly, the water content/potential of the soil has reached field capacity.

$$J_w|_{\psi_m = \psi_{m,fc}} = \text{water flux at field capacity} = -K(\psi_{m,fc}) \frac{d\psi_m}{dz} + g K(\psi_{m,fc})$$

small                      small                      small



$$\psi_{m,fc} = \text{matric potential at field capacity} = -30 \frac{J}{kg}$$

Note that  $J_w|_{\psi_{m,fc}} \neq 0$  since there will always be some water movement. Think of soil water as

being held by a leaky bucket. Hole in bucket through which water leaks changes as soil water content changes, and gets smaller rapidly near  $\psi_{m,fc}$ .  
*(large at high water content)*

21/3/2011  
31/03/2011

# Soil Water Evaporation

Optional 3/03/2011

vapor pressure of atmosphere compared to vapor pressure at soil surface

Evaporation occurs in 2 stages.

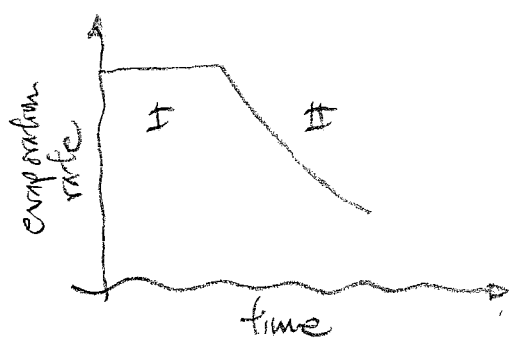
I) steady rate of evaporation, determined by evaporative demand of the atmosphere. Think of diffusion of water vapor at soil surface to atmosphere

II) falling rate of evaporation once the soil surface has dried, rate of evaporation now depends on ability of soil to move water to the surface.

$$E_{cum II} = \text{cumulative evaporation in stage II} \\ = C \sqrt{t - t_I}$$

$C = f(\text{soil type})$ ,  $t_I = \text{time stage I ends}$

recall  $I_w \sim \sqrt{t}$



## Transpiration and Plant Water Uptake

Water moves from the soil to plant roots, through the xylem, to the leaves, and then evaporates from the cavities of the stomata.

$$U_p^* = \frac{\text{dimensionless quantity}}{E_{p,max}} = \frac{U_p}{E_{p,max}} = \frac{\text{max potential water uptake by plant}}{\text{max possible transpiration}} = 1 - (1 + 1.3 A_w)^{-b}$$

determined mostly by atmosphere

$$A_w = \frac{\text{available water fraction}}{\theta_{fc} - \theta_{pwp}} = \frac{\theta - \theta_{pwp}}{\theta_{fc} - \theta_{pwp}}$$

$\theta_{pwp}$  = vol water content @ permanent wilting point

$\theta_{fc}$  = vol water content @ field capacity

$$[U_p] = [E_{p,max}] = \text{mm} \cdot \text{day}^{-1}$$

If ambient water vapor pressure is such that a plant is transpiring at  $E_{p,max}$ , then

$$U_p = [1 - (1 + 1.3 A_w)^{-b}] E_{p,max} \rightarrow \text{see Fig 9.9}$$

## Heat Pulse Measurements to determine:

- soil thermal properties
- soil water content
- infiltrating liquid water flux
- sensible heat flux in soil
- latent heat flux (vaporization or fusion)
- upward liquid water flux

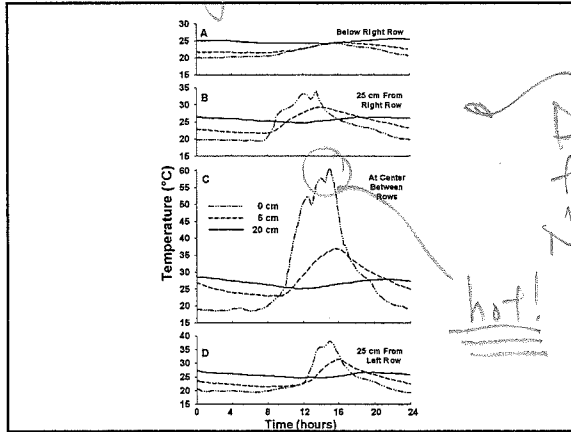
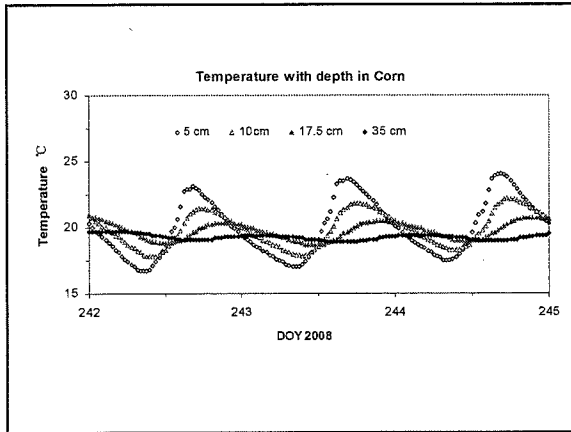
Agron 405/505

## Soil heat and water dynamics

- Impact biological, chemical, and physical, processes
- Modeling coupled heat and water dynamics is difficult and requires many hard to measure parameters
- Measuring in situ coupled heat and water dynamics has improved recently

spatial and temporal variability

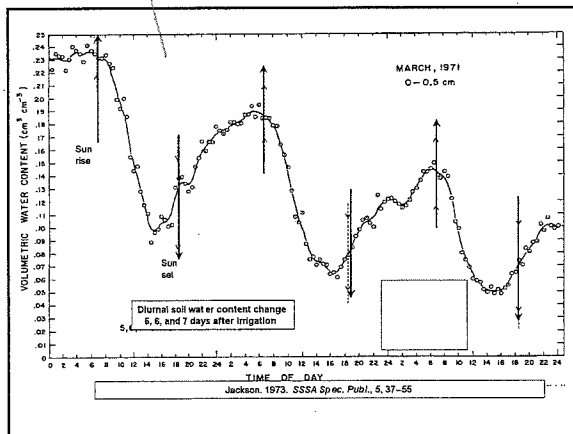
Research - improving models of soil heat and water flow  
Needs: good measurements!



from Dr. Horton's thesis, New Mexico

Use measurements to improve our understanding of physical processes

Ray Jackson, data from Arizona



occur simultaneously

## Coupled Heat and Water Transfer

Thermal gradients cause water to move in unsaturated soil.

When water moves in soil, it carries heat.

Because heat transfer and water movement affect one another they are coupled.

### Determining of soil thermal properties by heat pulse sensor

Soil thermal diffusivity  $\alpha$  ( $J/m^3 \cdot C$ )

$$\alpha = \frac{r^2}{4} \left[ \frac{1}{(t_m - t_0)} - \frac{1}{t_m} \right] \ln \left[ \frac{t_m}{(t_m - t_0)} \right]$$

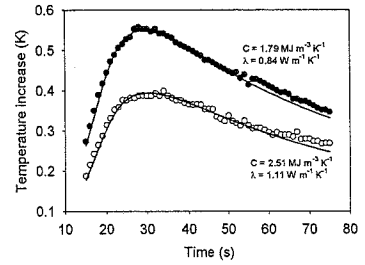
Soil heat capacity  $C$  ( $J/m^3 \cdot C$ ):

$$C = \rho c = \frac{t_0 q'}{e \pi r^2 \Delta T_m}$$

Soil thermal conductivity  $\lambda$  ( $W/m \cdot C$ ):

$$\lambda = \alpha C$$

### Example of heat pulse data

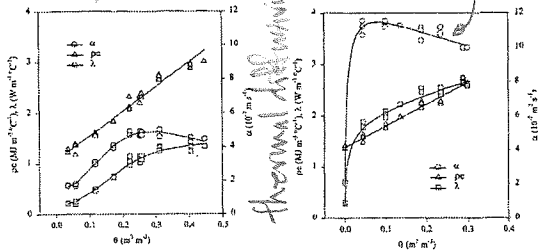


By fitting a heat transfer model to the heat pulse data we determine the soil thermal properties.

$C$  → volumetric heat capacity ( $J/m^3 \cdot C$ )  
 $\lambda$  → thermal conductivity ( $W/m \cdot C$ )  
 $\alpha$  → thermal diffusivity ( $K$ )

volumetric heat capacity

### Thermal properties



clay loam

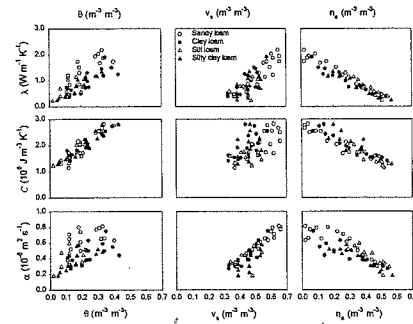
sand

water content

bulk density,  $k_g/m^3$

because expands

### Soil thermal properties

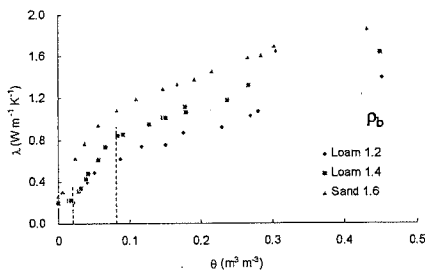


relate thermal properties to soil content

volume fraction of solids

volume fraction of air

### Influences of soil texture, $\rho_b$ and $\theta$ on $\lambda$

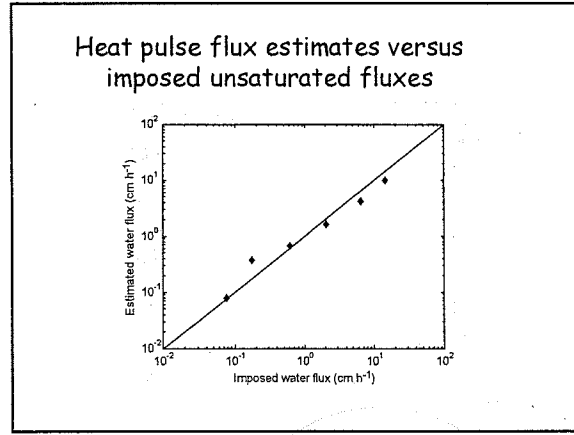
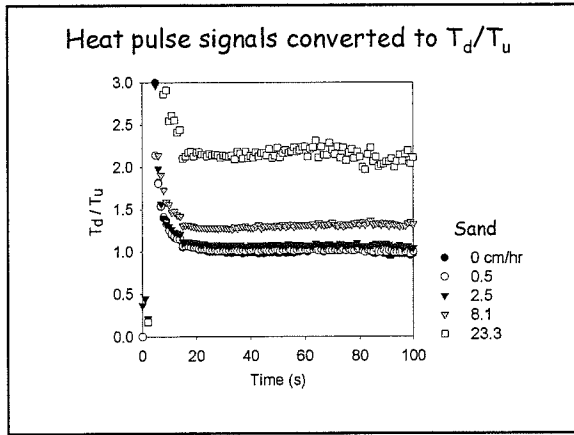
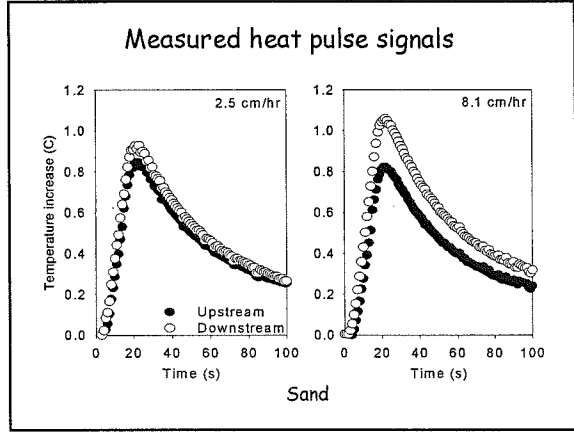
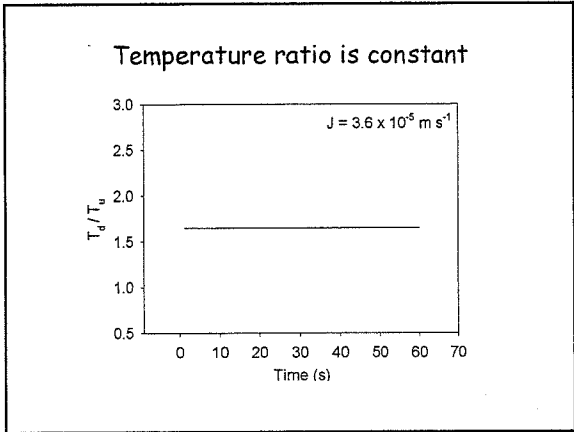


### Calculation of Volumetric Heat Capacity

$$\rho c = \rho_s c_s + \theta \rho_w c_w \quad (\text{ignore gas phase})$$

This equation can be used to estimate soil  $\rho_b$  or  $\theta$  with the heat-pulse technique.

If  $\rho_b$  doesn't change (soil doesn't shrink or swell)  $\theta$  can be inferred from  $\rho c_s$ .



$$H = -k \frac{\Delta T}{\Delta z}$$

A Heat Pulse Technique for Estimating Soil Water Evaporation

**Basic theory of HP method:**

Sensible heat balance provides a means to determine latent heat ( $LE$ ) used for evaporation.

$$LE = (H_1 - H_2) - \Delta S$$

$\left\{ \begin{array}{l} = 0 \text{ no evaporation} \\ > 0 \text{ evaporation} \\ < 0 \text{ condensation} \end{array} \right.$

Sensible heat flux in,  $H_1$

Sensible heat storage change  $\Delta S$

Sensible heat flux out,  $H_2$

$LE$

## Latent Heat in Soil Heat Flux Measurements

Which temperature should we be using to estimate evaporation? Surface? Subsurface?

## Better Energy Balance Closure

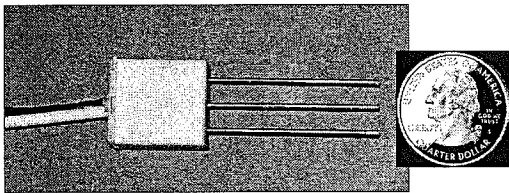
When the latent heat flux ( $LE$ ) includes evaporation from soil, the depth at which we measure soil heat flux ( $G$ ) is critical to accurately representing the surface energy balance.



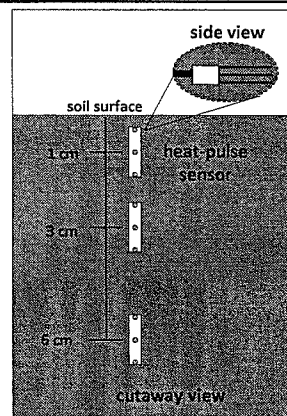
Objective: Characterize variations in  $G$  with depth near the soil surface.

## Materials and Methods

Soil heat flux ( $G$ ) measured via heat-pulse sensors installed at 3 depths: 1, 3, and 6 cm

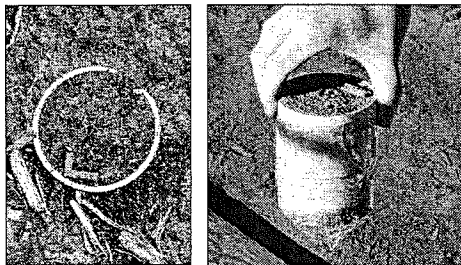


$$G = -\lambda(\Delta T/\Delta z)$$

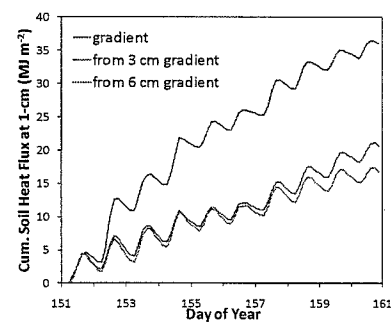


## Materials and Methods

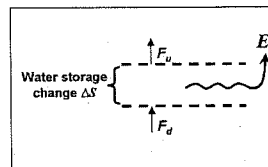
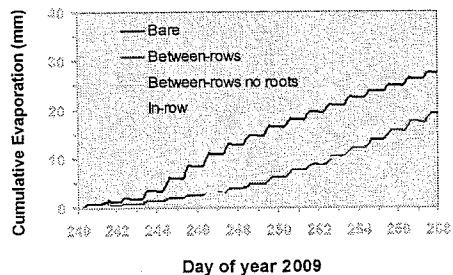
Evaporation ( $LE$ ) determined via microlysimeters (per 24 h)



## Cumulative Soil Heat Flux at 1-cm Depth



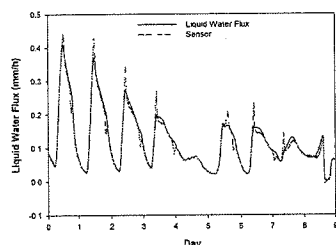
### Cumulative soil water evaporation at 3-mm soil depth



$$\Delta E = (F_d - F_b) + \Delta S$$

For a soil layer,  $\Delta E$  is the evaporation rate (cm/h),  $F_d$  and  $F_b$  are the liquid water flux (cm/h) at top and bottom boundaries, and  $\Delta S$  is the change in water storage (cm/h).

### Liquid water flux at the 7.5 mm soil depth from the model simulation.



### Conclusions

The heat pulse method is able to provide a wide range of soil heat and water measurements.

This is an important time period to advance coupled heat and water experiments and models.

### References

- Ren, T., G.J. Kluitenberg, and R. Horton. 2000. Determining soil water flux and pore water velocity by a heat pulse technique. *Soil Sci. Soc. Am. J.* 64:552-560.
- Wang, Q., T.E. Ochsner, and R. Horton. 2002. Mathematical analysis of heat pulse signals for soil water flux determination. *Water Resour. Res.* 38, DOI 10.1029/2001WR001089.
- Heitman, J.L., R. Horton, T.J. Sauer, and T.M. DeSutter, 2008. Sensible heat observations reveal soil water evaporation dynamics. *J. Hydrometeorol.*, 9: 165-171.
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- Xiao X., R. Horton, T.J. Sauer, J.L. Heitman and T. Ren, 2011. Cumulative soil water evaporation as a function of depth and time. *Vadose Zone J.* (in press).