

4) core mass flux eqn.

$$\dot{m}_c = \frac{\Gamma}{\sqrt{R}} \frac{\pi_e \pi_c \pi_r}{\sqrt{\tau_e \tau_r}} \frac{P_0}{\sqrt{T_0}} A_8 \quad (4)$$

π_e, τ_e, π_r and A_8 are known

so (4) is

$$F_4(\dot{m}_c, \pi_c, \tau_r) = 0 \quad (4)$$

(1) - (4) are 4 eqns with unknowns $\pi_c, \pi_{c1}, \tau_r, \alpha$ and $\dot{m}_c = 5$ unknowns

\Rightarrow need an additional eqn. (not obvious).
Really need compressor and fan maps in order to know how π_c is related to π_{c1} as engine rpm changes, i.e. to close the system, need

$$\pi_{c1} = \pi_c(\pi_c)$$

parameterized by rpm.

\Rightarrow soln. for $\pi_c, \pi_{c1}, \tau_r, \alpha$ + \dot{m}_c

$$\dot{m}_c + \dot{m}_F = \frac{\Gamma}{\sqrt{R}} \frac{P_0}{\sqrt{T_0}} \left\{ \frac{\pi_e \pi_c \pi_r}{\sqrt{\tau_e \tau_r}} + \frac{\pi_{c1} \pi_r}{\sqrt{\tau_{c1} \tau_r}} A_8 \right\} A_8$$

all known