

$$2 \tau_r \tau_c = \tau_a + \tau_r$$

$$\tau_c = \frac{\tau_a + \tau_r}{2 \tau_r}$$

then

$$\tau_t = 1 - \frac{\tau_r}{\tau_a} (\tau_c - 1) = 1 - \frac{\tau_r}{\tau_a} \left(\frac{\tau_a + \tau_r - 2 \tau_r}{2 \tau_r} \right)$$

$$\tau_t = 1 - \frac{\tau_a - \tau_r}{2 \tau_a} = \frac{2 \tau_a - \tau_a + \tau_r}{2 \tau_a}$$

$$\tau_t = \frac{\tau_a + \tau_r}{2 \tau_a}$$

specific thrust

$$\frac{F}{\dot{m}} = a_0 \left\{ \left[\frac{2}{\gamma - 1} \frac{\tau_{TAB}}{\tau_r \tau_c \tau_t} (\tau_r \tau_c \tau_t - 1) \right]^{\frac{1}{2}} - M_0 \right\}$$

$$\frac{F}{\dot{m}} = a_0 \left\{ \left[\frac{2 \tau_{TAB}}{\gamma - 1} \left(1 - \frac{1}{\tau_r \tau_c \tau_t} \right) \right]^{\frac{1}{2}} - M_0 \right\}$$

$$\tau_r \tau_c \tau_t = \tau_r \left(\frac{\tau_a + \tau_r}{2 \tau_r} \right) \left(\frac{\tau_a + \tau_r}{2 \tau_a} \right) = \frac{(\tau_a + \tau_r)^2}{4 \tau_a}$$