

**IE 361 Exam 2**  
**(With "Clarified Version" of Question #3)**  
**Fall 2007**

**I have neither given nor received unauthorized assistance on this exam.**

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Name

Date

This exam consists of 20 multiple choice questions. There is a single best answer for each question. Circle **EXACTLY ONE** response for each question on this answer sheet.

- 1.    A    B    C    D    E
- 2.    A    B    C    D    E
- 3.    A    B    C    D    E
- 4.    A    B    C    D    E
- 5.    A    B    C    D    E
- 6.    A    B    C    D    E
- 7.    A    B    C    D    E
- 8.    A    B    C    D    E
- 9.    A    B    C    D    E
- 10.   A    B    C    D    E
- 11.   A    B    C    D    E
- 12.   A    B    C    D    E
- 13.   A    B    C    D    E
- 14.   A    B    C    D    E
- 15.   A    B    C    D    E
- 16.   A    B    C    D    E
- 17.   A    B    C    D    E
- 18.   A    B    C    D    E
- 19.   A    B    C    D    E
- 20.   A    B    C    D    E

1. Control charting
  - a) is a form of Engineering Feedback Control.
  - b) compares individual process measurements to specifications in order to check for lack of process stability.
  - c) is most effective as a quality assurance tool when applied at the end of a production chain, a substantial distance in time and space from processes being monitored.
  - d) None of responses a) through c) are correct completions of the sentence.
  - e) Exactly 2 of responses a) through c) are correct completions of the sentence.
  
2. Control limits for a generic plotted statistic  $Q$ 
  - a) are typically derived from a probability model for  $Q$  appropriate when individual process outcomes are modeled as "independent draws from a fixed universe."
  - b) typically depend upon the size of the sample used to compute  $Q$ .
  - c) typically depend upon process parameters.
  - d) All of responses a) through c) are correct completions of the sentence.
  - e) Exactly 2 of responses a) through c) are correct completions of the sentence.
  
3. In standards-given variables control charting with sample size  $n$  and process standards  $\mu$  and  $\sigma$ ,
  - a) the difference between  $UCL_{\bar{x}}$  and  $LCL_{\bar{x}}$  **always** shrinks as  $n$  increases (the spread in control limits gets smaller as sample size increases).
  - b) the difference between  $UCL_s$  and  $LCL_s$  **always** shrinks as  $n \geq 6$  increases (the spread in control limits gets smaller as sample size increases).
  - c) the difference between  $UCL_R$  and  $LCL_R$  **always** shrinks as  $n \geq 7$  increases (the spread in control limits gets smaller as sample size increases).
  - d) All of responses a) through c) are correct completions of the sentence.
  - e) Exactly 2 of responses a) and b) are correct completions of the sentence.

Below are sample means and ranges from 10 samples of size  $n = 5$ . Use the information from these samples to answer questions 4 through 6.

Sample	1	2	3	4	5	6	7	8	9	10	Sum
$\bar{x}$	11.0	11.9	9.7	10.0	11.1	11.3	11.0	11.5	11.1	12.6	111.2
$R$	2.1	6.0	3.9	4.5	3.9	5.8	6.0	5.2	2.9	6.8	47.1

4. Consider standards given control charting for both  $\bar{x}$  and  $R$ , with standards  $\mu = 11.0$  and  $\sigma = 2.0$ .
  - a) The  $\bar{x}$  chart and  $R$  chart both produce out-of-control signals.
  - b) The  $\bar{x}$  chart produces out-of-control signals, but the  $R$  chart does not.
  - c) The  $\bar{x}$  chart produces no out-of-control signals, but the  $R$  chart produces signals.
  - d) Neither chart produces out-of-control signals.
  
5. Consider retrospective control charting for both  $\bar{x}$  and  $R$ .
  - a) The  $\bar{x}$  chart and  $R$  chart both produce out-of-control signals.
  - b) The  $\bar{x}$  chart produces out-of-control signals, but the  $R$  chart does not.
  - c) The  $\bar{x}$  chart produces no out-of-control signals, but the  $R$  chart produces signals.
  - d) Neither chart produces out-of-control signals.

6. Ignore any lack of stability that you may have found in the sample ranges on the previous page and use the values there to estimate  $\sigma$ . Based on this estimate, in turn set an upper control limit for the sample standard deviation ( $s$ ) for an additional sample of size  $n = 4$ . (Remember that the samples represented in the table were of size  $n = 5$ .) This limit is closest to

- a) 2.02.
- b) 3.98.
- c) 4.23.
- d) 9.51.
- e) 9.96.

7. Below are 3 statements about control charting. How many of them are true?

- $R$  charting is less sensitive to process change than  $s$  charting.
  - Small sample sizes deprive one of the possibility of directly detecting unexpected improvements in process "spread" using ordinary three-sigma Shewhart control charts.
  - If one uses only an  $\bar{x}$  chart (and no  $R$  or  $s$  chart) it is impossible to detect a huge increase in process "spread."
- a) All 3 are correct.
  - b) Exactly 2 are correct.
  - c) Exactly 1 is correct.
  - d) None is correct.

8. In a particular "mean nonconformities per unit" context, a process standard rate is 1.5 nonconformities per single inspection unit. A redesign of some elements of the production process is intended to reduce that rate/improve the process. After implementation of the redesign, a standards given Shewhart control charting scheme will be set up to monitor nonconformities per unit based on  $k$  inspection units per sampling period.

- a) *Neither* a  $k = 2$  scheme nor a  $k = 8$  scheme *will* provide the ability to directly confirm a process improvement.
- b) A  $k = 2$  scheme *will not* provide the ability to directly confirm a process improvement, but a  $k = 8$  scheme *will* provide this ability.
- c) A  $k = 2$  scheme *will* provide the ability to directly confirm a process improvement, but a  $k = 8$  scheme *will not* provide this ability.
- d) *Both* a  $k = 2$  scheme and a  $k = 8$  scheme *will* provide the ability to directly confirm a process improvement.
- e) Not enough information is given here to tell whether any particular choice of  $k$  will provide the possibility of directly confirming process improvement.

9. Below are some records from inspection for counts of loose bolts (after torquing) on a model of large machine. (Each machine has 120 such bolts that are all checked.)

Machine	1	2	3	4	5	6	7	8	9	10	Sum
Loose Bolts	11	6	6	7	8	6	6	10	5	9	74

Appropriate retrospective control limits for the counts in the table above

- a) are  $7.4 \pm 7.9$ .
- b) are  $7.4 \pm 8.2$ .
- c) indicate process stability.
- d) a) and c) are both correct completions of the sentence.
- e) b) and c) are both correct completions of the sentence.

10. Standards given control limits for  $\bar{x}$  based on samples of size  $n = 5$  are  $17 \pm 2$ .
- Corresponding standards given control limits for sample medians are  $17 \pm 2.4$ .
  - Corresponding engineering specifications on  $x$  must be  $17 \pm 2.7$ .
  - Corresponding standards given control limits for  $s$  are impossible to determined based on this information.
  - Exactly 2 of a) through c) are correct completions of the sentence.
  - All of a) through c) are correct completions of the sentence.
11. Plotted points "hugging the center line" on a Shewhart  $\bar{x}$  chart
- could be produced by an unexpected decrease in the process standard deviation,  $\sigma$ .
  - are the ideal, indicating a very stable process.
  - will fail to be directly detected by any of the "Western Electric Alarm Rules."
  - Exactly 2 of a) through c) are correct completions of the sentence.
  - All of a) through c) are correct completions of the sentence.
12. Five nominally identical production streams
- should be treated as a single stream for purposes of process monitoring.
  - can produce a "rational subgroup" if one outcome is sampled from each stream at a given period.
  - are best monitored using 5 separate control charts.
  - Exactly 2 of a) through c) are correct completions of the sentence.
  - All of a) through c) are correct completions of the sentence.
13. Process standards are  $\mu = 100$  and  $\sigma = 7$  and observations from the process are normally distributed. Below are 3 statements about a standards-given Shewhart  $\bar{x}$  chart for this process. How many of them are true?
- The chart has the same ARL when  $\mu = 100$  and  $\sigma = 7$  as does a standards given  $\bar{x}$  chart for a process with standards  $\mu = 15$  and  $\sigma = .7$  when in fact  $\mu = 15$  and  $\sigma = .7$ .
  - The ARL for this chart when  $\mu = 100$  and  $\sigma = 5$  is more than 370.
  - The ARL for this chart when  $\mu = 100$  and  $\sigma = 9$  is less than 370.
- All 3 are correct.
  - Exactly 2 are correct.
  - Exactly 1 is correct.
  - None is correct.
14. Flaws are generated in the production of carpet at a standard rate of 1 per 20 square yards of carpet. Certain 5 square yard rugs are inspected for flaws and a rug is considered to be non-conforming if it has any flaws on it. 10 of these rugs are inspected per hour. Let
- $X$  = the total number of flaws seen across the 10 rugs, and
- $Y$  = the number of non-conforming rugs among the 10
- Standards given control limits for  $X$  and  $Y$  are
- respectively  $2.5 \pm 4.7$  and  $2.5 \pm 4.1$ .
  - respectively  $2.5 \pm 4.7$  and  $2.2 \pm 4.5$ .
  - respectively  $2.5 \pm 4.7$  and  $2.2 \pm 3.9$ .
  - impossible to determine from the given information.
  - None of a) through d) is a correct completion of the sentence.

15. "Online"/ongoing process tweaking/adjustment
- is never an appropriate variation reduction methodology.
  - requires having a process "knob" that one can "turn" with predictable results in response to a process mis-adjustment.
  - is an alternative to control charting (having the same realm of application as Shewhart charting).
  - None of a) through c) is a correct completion of the sentence.
  - Exactly 2 of a) through c) are correct completions of the sentence.

16. 10 consecutive samples of size  $n = 1$  from a process are as below

Sample	1	2	3	4	5	6	7	8	9	10	Mean
$x$	1.01	2.03	2.98	3.97	4.95	5.97	6.97	8.07	8.96	9.97	5.488
$MR$		1.02	.95	.99	.98	1.02	1.00	1.10	.89	1.01	.9956

Further,

$$.9956 / 1.128 = .883$$

- A retrospective individuals chart based on the best available estimate of  $\sigma$  indicates there is process instability, and this estimate and analysis appear to be appropriate.
  - A retrospective individuals chart based on the best available estimate of  $\sigma$  indicates no process instability, and this estimate and analysis appear to be appropriate.
  - A retrospective individuals chart based on the best available estimate of  $\sigma$  indicates there is process instability, but the clear linear trend in the data makes it clear that this estimate is inappropriate.
  - A retrospective individuals chart based on the best available estimate of  $\sigma$  indicates no process instability, but the clear linear trend in the data makes it clear that this estimate is inappropriate.
17. Normal plots (normal quantile plots in JMP language)
- will always be approximately linear if a sample of size at least 30 is represented.
  - are tools for assessing the extent to which one should trust the confidence levels associated with the intervals for  $6\sigma$ ,  $C_p$ , and  $C_{pk}$  and the normal-based prediction and tolerance intervals of Chapter 5 of *SQAME*.
  - are tools for assessing whether  $C_p$  and  $C_{pk}$  are relevant descriptors of process capability.
  - Exactly 2 of responses a) through c) are correct.
  - All of responses a) through c) are correct.

Data from problem 5.15 of *SQAME* include measured diameters from  $n = 20$  3-inch rolled sheet metal saddles produced on a single day. These have  $\bar{x} = 3.0377$  in,  $s = .0606$  in,  $\min x_i = 2.969$  in, and  $\max x_i = 3.188$  in. Specifications on this diameter are  $3.00 \pm .20$  in. Use these facts to answer questions 18 through 20.

18. Assuming diameter to be normally distributed, what are limits that you are "at least 90% sure" would bracket one more (a 21<sup>st</sup>) saddle diameter?
- 2.969 in and 3.118 in.
  - $3.0377 \pm .1074$  in.
  - $3.0377 \pm .0606$  in.
  - either response a) or response b) could be correctly used.
  - either response a) or response c) could be correctly used.

19. If one assumes that the saddle-rolling process produces normally distributed diameters, 95% confidence limits for a capability ratio measuring current process performance
- a) are .57 and 1.21.
  - b) are .75 and 1.45 .
  - c) could be used to help evaluate whether a company "Six Sigma Program" goal is being met by seeing where the limits are relative to the value 2.0.
  - d) Both a) and c) are correct completions of the sentence.
  - e) Both b) and c) are correct completions of the sentence
20. Assuming diameter to be normally distributed, 95% confidence limits for the "process capability,"  $6\sigma$
- a) are .28 in and .53 in .
  - b) are .21 in and .77 in .
  - c) are .05 in and .09 in .
  - d) can not be determined from the information provided.
  - e) can be determined from the information provided, but are not close to any of the limits provided in a) through c).